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**SIGNAL  
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Editorial

Fractional signal processing and applications

1  
3 The term “fractional” emerged in recent years in  
4 connection with different signal processing theories  
5 and techniques, sometimes with no visible connection  
6 between them. Nevertheless, the first reference to this  
7 area appeared during 1695 in a letter from Bernoulli  
8 to Leibnitz, where he formulated a question about the  
9 meaning of a non-integer order derivative. It was the  
10 beginning genesis of the Fractional Calculus that is  
11 the root of the continuous-time fractional systems de-  
12 scribed by fractional differential equations. Since then,  
13 Fractional Calculus (FC) evolved through the contri-  
14 butions of many famous mathematicians. In spite of  
15 the progress in pure mathematics, we had to wait up  
16 to the 1920s, during the 20th century, for the appear-  
17 ance of studies concerning the use of FC in Applied  
18 Sciences. Furthermore, only in the last three decades  
19 the application of FC engineering deserved attention,  
20 motivated by the works of Mandelbrot on Fractals,  
21 that led to a significant impact in several scientific  
22 areas and attracted, definitively, the attention to frac-  
23 tional “objects”. Presently, new themes are the object  
24 of active research such as, fractional Brownian mo-  
25 tion, discrete-time fractional linear systems, fractional  
26 delay filtering, fractional splines and wavelets.

27 In a similar line of thought, we can mention the  
28 concept of fractional fourier transform (FF) that was  
29 first introduced in 1929 in the area of mathematics.  
30 More recently, in 1980, this tool was rediscovered by  
31 the physicist Namias based on the spectral structure  
32 of the classical fourier transform. Most reported ap-  
33 plications on FF are in the field of optics but other  
34 topics in signal analysis have appeared in the lit-  
35 erature, namely filtering, encoding, watermarking,  
36 phase retrieval and others. While FC and FF consti-  
37 tute distinct mathematical formalisms some results  
38 point out that a common paradigm can be achieved,  
39 although not totally clear at the present state of  
affairs.

Bearing these facts in mind, we felt that it was the  
time for establishing a special issue on the application  
of FC and FF concepts in areas related to signal pro-  
cessing. We believe that the contributions gathered in  
this issue give, not only a good overview on the state  
of application of FC and FF, but also point out new  
directions of future research and development. Con-  
sequently, in order to guide the reader throughout the  
issue we have grouped the articles in five major areas,  
leading from theoretical aspects up to more applied  
studies as listed in the sequel.

**Theoretical achievements in fractional calculus**

T.T. Hartley and C.F. Lorenzo introduce the con-  
cept of continuous-order distribution and discuss its  
application in the identification of fractional and inter-  
ger order systems.

M. Ortigueira studies the initial condition prob-  
lem for fractional linear system and extends the  
well-known result obtained by the Laplace Trans-  
form, being the most interesting feature its indepen-  
dence upon the derivative definition. In a second  
paper, the same author proposes a new definition for  
a symmetric fractional B-spline that constitutes the  
generalization of the usual integer order B-spline.

**Continuous-time realization and approximation**

T. Poinot and J.-C. Trigeassou describe a method for  
the modelling and simulation of fractional systems, by  
adopting a state-space representation where the con-  
ventional integration is replaced by a fractional one.

N. Guijarro and G. Dauphin-Tanguy present a  
method for the approximation, reduction and real-  
ization of a class of fractional models. The method

1 is based on the interconnection of passive elementary blocks, leading to a finite-dimensional passive  
 3 approximate model that can be reduced through a Krylov–Lanczos process. Finally, a bond graph realization  
 5 of this reduced order model is given.

7 N. Heymans addresses hierarchical viscoelastic elements whose behaviour is intermediate between  
 9 linear elasticity and Newtonian viscosity (spring pots). Such elements are incorporated into classical  
 11 analogue models describing linear viscoelastic behaviour and the approach is extended to characterize  
 13 the terminal transition from self-similar viscoelasticity up to pure flow.

### Discrete-time realization and approximation

15 The very important topic of discrete-time realization and approximation of fractional systems is considered  
 17 in the papers of Y. Chen and B.M. Vinagre and P. Ostalczyk, respectively. In the first article a discrete-time  
 19 fractional differentiator is proposed by using a new family of first-order differentiators expressed in the  
 21 pole-zero form. In the second study different types of discrete-time integrators and distinct orders of  
 23 integration are considered. Their transient and frequency characteristics are also discussed.

### Applications of fractional linear systems

27 *Robotics:* E.S. Pires, J.T. Machado, and P.M. Oliveira address the problem of signal propagation and  
 29 fractional-order dynamics during the evolution of a genetic algorithm (GA) for generating robot manipulator  
 trajectories.

31 P. Melchior, B. Orsoni, A. Poty, O. Laviolle, and A. Oustaloup present a comparison between two optimization  
 33 methods for mobile robot path planning adopting a fractional potential. A fractional-order map of danger  
 35 is embedded into A\* and Fast Marching techniques for a vehicle path planning in an environment with  
 37 fixed obstacles.

39 *Diffusion:* J.R. Leith studies the fractal growth of fractional diffusion from the viewpoint of the fractional  
 41 derivative order influence on the scaling exponents. R. Gorenflo and A. Vivoli present another

perspective and develop a theory of discrete-space discrete-time random walks, analogous to the theory  
 of continuous-time random walks for space-time fractional diffusion equations

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 45  
 47 *Other:* B. Mathieu, P. Melchior, A. Oustaloup, and Ch. Ceyral apply the fractional derivative in Image  
 49 Processing by presenting a method for edge detection. On the other hand, R.R. Nigmatullin and S.I. Osokin  
 51 present a complex permittivity model for dielectric asymmetric spectra description in dielectric spectroscopy  
 53 signal processing.

### Fractional fourier transform and applications

C. Candan and H.M. Ozaktas present new derivations of some sampling relations and series expansions  
 for FF and other transforms. The method can also be applied to the Fresnel, Hartley, scale transform, and  
 similar transforms.

L. Stankovic, T. Alieva, and M.J. Bastiaans propose a Wigner relative time-frequency distribution based on  
 a fractional-Fourier-domain realization. This approach has the advantage of having reduced cross-terms and  
 is generalized to the time-frequency distributions from the Cohen class.

G. Gonon, O. Richoux, and Claude Depollier use the FF transform to estimate the parameters of linear  
 chirps. The authors adopt a filtering in the fractional domain and are successful in extracting linear chirps  
 out of a multi-component noisy signal. The method is used to analyse the propagation of acoustic waves in  
 a dispersive medium.

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