



discharge voltage droop.

The concept of resonant voltage droop compensation consists in taking advantage of the almost linear part of the sine waveform of the capacitor  $C_r$  voltage, where (1) holds.

$$\sin(\alpha) \approx \alpha \quad \Rightarrow \quad -\pi/6 < \alpha < \pi/6 \quad (1)$$

In order to use only part of the almost linear area of the sine waveform, it was considered that pulses starts at zero resonant voltage, as shown in Fig. 3.

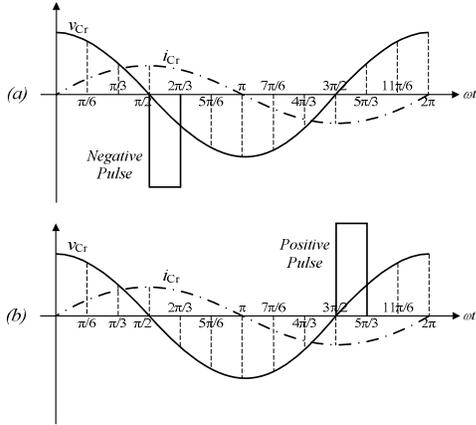


Fig. 3. Resonant circuit voltage and current waveforms and (a) negative and (b) positive pulse starting at zero resonant voltage under almost linear part of the sine waveform.

## II. CIRCUIT OPERATION

Fig. 2 shows the proposed circuit topology to deliver repetitive unipolar or bipolar high-voltage output pulses with compensation, comprising  $n$  stages and one voltage droop compensation stage, with IGBTs as on-off switches. The circuit of Fig. 2 presents several operating modes. The first one consists in charging the capacitors  $C_i$  and  $C_r$  through the path consisting by switches  $T_{dc}$ ,  $D_{dc}$ ,  $T_{a\_res}$ ,  $T_{ai}$ ,  $D_{b\_res}$ ,  $D_{bi}$ ,  $D_{g\_res}$ ,  $D_{gi}$ ,  $T_{e\_res}$  and  $T_{ei}$  on and all others switches off, as shown in Fig. 4. The next operating mode depends on the required output characteristic imposed by the load. Thus, before applying negative or positive pulse with compensation into a load, it is necessary to trigger on switches,  $T_{a\_res}$  and  $T_{c\_res}$  to connect the capacitor  $C_r$  in series with inductor  $L_r$  to start the resonance through its single cycle sine wave, as shown in Fig. 3. To apply negative pulse with compensation accordingly with Fig. 3a), switches  $T_{bi}$  and  $T_{ci}$  are turned on at  $\alpha = \pi/2$  (zero resonant voltage). After negative pulse, turning off switches  $T_{a\_res}$  and  $T_{c\_res}$  must obey the condition in (2), assuring the continuity of the current and recovery of the energy in inductor  $L_r$  back to capacitor  $C_r$ , as can be seen in Fig. 3a) and Fig. 4.

$$\pi < \omega\tau < 2\pi \quad (2)$$

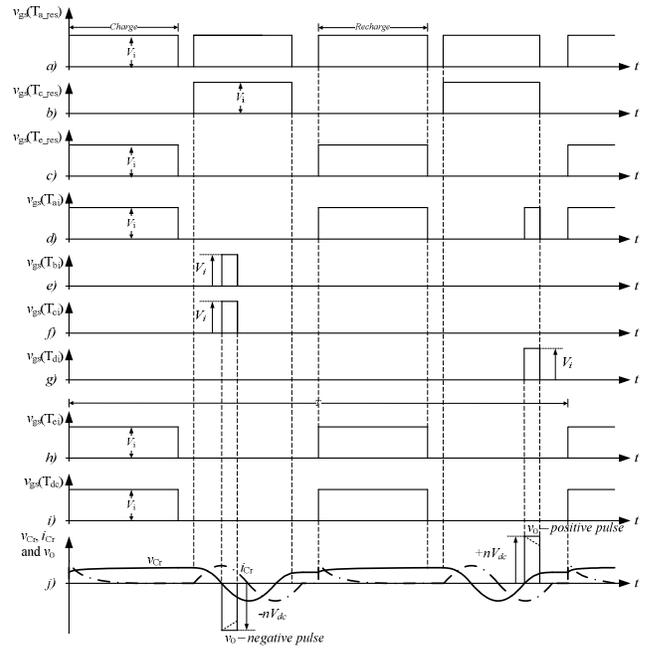


Fig. 4. Theoretical wave forms for the operation of the  $S^2BM$  of Fig. 2, considering a resistive load. Drive signal of semiconductors: a)  $T_{a\_res}$ ; b)  $T_{c\_res}$ ; c)  $T_{ai}$ ; d)  $T_{bi}$ ; e)  $T_{ci}$ ; f)  $T_{di}$ ; g)  $T_{ei}$ ; h)  $T_{dc}$ ; i)  $v_{Cr}$ ,  $i_{Cr}$  and output  $v_0$  voltage.

The positive pulse with compensation can be obtained (assuming that capacitor  $C_r$  is previously connected in series with inductor  $L_r$ , see Fig. 3b)) by switching on  $T_{ai}$  and  $T_{di}$  at  $\alpha = 3\pi/2$  after starting the resonance. After the positive pulse, switches  $T_{a\_res}$  and  $T_{c\_res}$  can be turned off safely because the freewheeling diodes of these switches will assure the continuity of the current and recovery of the energy in inductor  $L_r$  back to capacitor  $C_r$ , as shown in Fig. 3 b) and Fig. 4.

## III. RESONANT PARAMETERS

In the resonant voltage droop compensation stage the capacitor  $C_r$  has same capacitance of Marx stages capacitors  $C_i$ . The inductance  $L_r$  was calculated taking into account the RLC series equivalent of the resonant circuit. Thus, solving the generic solution of RLC series circuit, (3) is obtained considering that the resistive part (the *on* resistance of the semiconductors) is negligible and the initial conditions of the capacitor  $C_r$  voltage and inductor  $L_r$  current are  $V_{dc}$  and zero respectively.

$$i_{L_r} = V_{dc} \sin(\omega_0 t) / (L_r \omega_0) \quad (3)$$

The inductance  $L_r$  was obtained, (4), considering that the negative and positive pulses lengths are restrained into intervals given by (5) and (6), for negative and positive pulse respectively, (Fig. 3).

$$L_r > 36t_{on}^2 / (\pi^2 C_r) \quad (4)$$

$$\pi/2 < \alpha < 2\pi/3 \quad (5)$$

$$3\pi/2 < \alpha < 5\pi/3 \quad (6)$$

#### IV. RESULTS

A laboratory prototype with five stages of the circuit presented in Fig. 2 was assembled using 1200 V IGBTs (SKW15N120) and diodes (IDB09E120), 4.5  $\mu\text{F}$  for main capacitors and capacitor  $C_r$ , 8 mH for inductor  $L_r$ , operating with 50 Hz pulse repetition rate, giving 1 kV bipolar pulses, with 100  $\mu\text{s}$  pulse width, and 9.5 ms relaxation time (i.e. time between negative and positive pulses) into resistive load.

Fig. 5 a) and b) shows the experimental results for the output voltage  $v_0$ , into the load, without compensation and 10% voltage droop at the end of the negative and positive pulses.

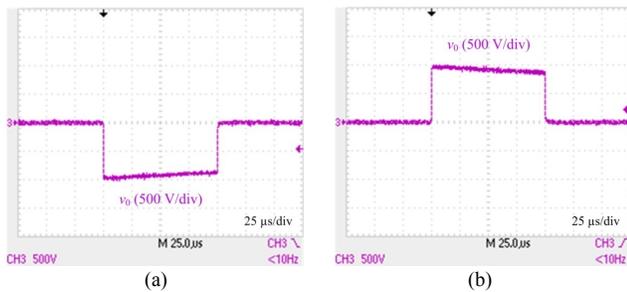


Fig. 5. Experimental results for the output voltage of the Fig. 2 circuit, into the load, without compensation and 10% voltage droop at the end of the negative (a) and positive (b) pulse. The scales are 25  $\mu\text{s}/\text{div}$  (horizontal) and 500 V/div (vertical).

Fig. 6 a) and b) shows the experimental results for the capacitor  $C_r$  voltage, current in inductor  $L_r$  and the output  $v_0$  voltage with compensation.

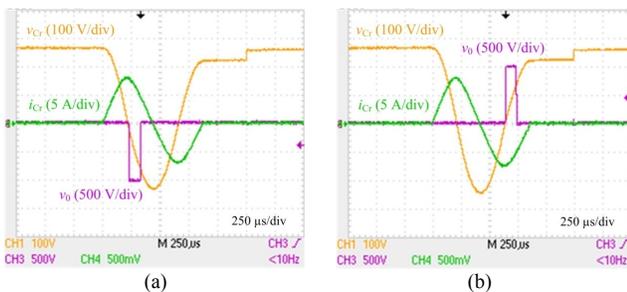


Fig. 6. Experimental results for the capacitor  $C_r$  voltage,  $v_{Cr}$ , current in inductor  $L_r$   $i_{Lr}$ , and the output  $v_0$  voltage with compensation of the circuit of Fig. 2, for negative (a) and positive (b) pulse. The scales are 250  $\mu\text{s}/\text{div}$  (horizontal) and 100 V/div (vertical).

In Fig. 7 a) and b) it is shown the experimental results of the output negative and positive pulse voltage with voltage droop compensation with zoomed horizontal scale.

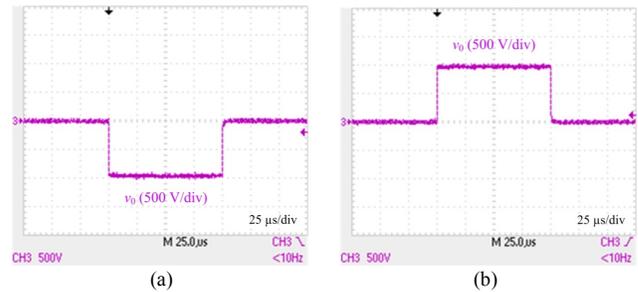


Fig. 7. Experimental results of the obtained output (a) negative and (b) positive pulse voltage with resonant compensation with zoomed horizontal scale, 25  $\mu\text{s}/\text{div}$  (horizontal) and 500V/div (vertical).

#### V. CONCLUSIONS

A new design scheme for voltage droop compensation based on resonant circuit in generalized solid-state bipolar Marx modulator of Fig. 2 was proposed for high-voltage repetitive pulsed power applications.

Keeping the topology of the Marx circuit, an auxiliary stage with inductor was added to the existing Marx stages, which compensates both the positive and negative output pulses. One characteristic of this scheme of compensation is the compromise between pulse repetition rate and the resonant frequency. Other aspect of the circuit of Fig. 2 is that the semiconductor  $T_{dc}$  has to hold-off two times the power supply voltage amplitude,  $V_{dc}$ . However, the presented topology avoids the need for auxiliary power supply to charge the capacitor of the voltage droop compensation stage, for both the positive and negative voltage pulses. The experimental results obtained from a laboratory prototype, for bipolar output voltage  $v_0$  into a resistive load, shows that the resonant based voltage droop compensation stage is able to compensate a 10% voltage droop both on the negative and positive pulses.

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